

WARM UP

Try another one... find the equation of the tangent and normal lines for when $f(x) = \sqrt{x}$ and $x=3$

slope

$$f(x) = \sqrt{x}$$

$$f(x) = x^{\frac{1}{2}}$$

$$f'(x) = \frac{1}{2}x^{-\frac{1}{2}}$$

$$f'(3) = \frac{1}{2}(3)^{-\frac{1}{2}}$$

$$f'(3) = \frac{1}{2} \cdot \frac{1}{\sqrt{3}}$$

$$m = \frac{1}{2\sqrt{3}}$$

tangent: $y - \sqrt{3} = \frac{1}{2\sqrt{3}}(x - 3)$

normal line: $y - \sqrt{3} = -2\sqrt{3}(x - 3)$

point

$$x = 3$$

$$f(3) = \sqrt{3}$$

$$(3, \sqrt{3})$$

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Chain Rule

Chain rule is used when a function is really a composition of two functions.

if $y = f(g(x))$ then

$$y' = f'(g(x)) g'(x)$$



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Chain Rule

For Example:

$$y = (x^2 + 7x)^4$$

$$\begin{array}{c} 4 \\ \text{---} \\ 4 \text{---} 3 \end{array}$$

$$\text{then } y' = 4(x^2 + 7x)^3 (2x + 7)$$

$$= (8x + 28)(x^2 + 7x)^3$$



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Sometimes you will see the rule written like this:

$$\text{if } y = \underline{u}(\underline{v(x)}) \quad \text{then}$$

$$y' = \underline{u}'(\underline{v(x)}) \underline{v}'(x)$$



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$$f(x) = (3x-1)^8$$

$$f'(x) = \underline{8} (3x-1)^7 (\underline{3})$$

$$f'(x) = \underline{24} (3x-1)^7$$



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$$f(x) = \frac{1}{\sqrt{x^2-5x}}$$

$$f(x) = (x^2-5x)^{-1/2}$$

$$f'(x) = -\frac{1}{2} (x^2-5x)^{-3/2} (\underline{2x-5})$$



$$= -\frac{(2x-5)}{2} (x^2-5x)^{-3/2}$$

$$= \frac{5-2x}{2} (x^2-5x)^{-3/2}$$

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Homework: p 217 #s 1-10 all

Exercise 7K

Each function is in the form $f(x) = u(v(x))$.

Identify $u(x)$ and $v(x)$, then find the derivative of f .

1 $f(x) = (3x^4 + 2x)^5$

2 $f(x) = 4(2x^2 + 3x + 1)^3$

3 $f(x) = \ln(3x^5)$

4 $f(x) = \sqrt[3]{2x + 3}$

5 $f(x) = e^{4x}$

6 $f(x) = (\ln x)^3$

7 $f(x) = (9x + 2)^{\frac{2}{3}}$

8 $f(x) = \sqrt[4]{2x^2 + 3}$

9 $f(x) = 5(x^3 + 3x)^4$

10 $f(x) = e^{4x^3}$



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