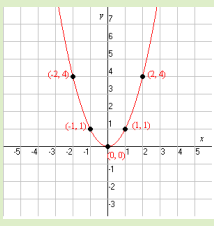


Use a GDC to examine each function graphically and numerically. Find the limit or state that it does not exist.

a $\lim_{x \rightarrow 2} x^2$ b $\lim_{x \rightarrow 1} \frac{x^2 - 1}{x - 1}$ c $\lim_{x \rightarrow 0} f(x)$; where $f(x) = \begin{cases} 1 & \text{for } x \geq 0 \\ -1 & \text{for } x < 0 \end{cases}$

a.)



Answers

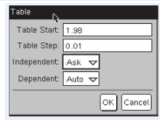
a $\lim_{x \rightarrow 2} x^2$

Plot the graph of $f(x) = x^2$ using a GDC, and look at the values of $f(x)$ as x approaches 2 from the right and from the left.

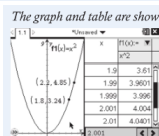
Graphically, $f(x)$ approaches 4 as x approaches 2.
Numerically, as x becomes close to 2 from either side, $f(x)$ becomes close to 4.

x	1.8	1.9	1.99	1.999	2.001	2.01	2.1	2.2
$f(x)$	3.24	3.61	3.960	3.996	4.004	4.040	4.41	4.84

To build the table above using a GDC, enter $f(x) = x^2$. Then set the independent variables to 'Ask'. Enter the values for x .



The graph and table are shown on the same screen.



For $f(x) = x^2$ we can substitute and find that $\lim_{x \rightarrow 2} x^2 = 2^2 = 4$

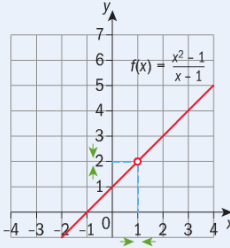
Feb 24-10:13 AM

Use a GDC to examine each function graphically and numerically. Find the limit or state that it does not exist.

a $\lim_{x \rightarrow 2} x^2$ b $\lim_{x \rightarrow 1} \frac{x^2 - 1}{x - 1}$ c $\lim_{x \rightarrow 0} f(x)$; where $f(x) = \begin{cases} 1 & \text{for } x \geq 0 \\ -1 & \text{for } x < 0 \end{cases}$

b.)

$\lim_{x \rightarrow 1^-} f(x) = 2$
 $\lim_{x \rightarrow 1^+} f(x) = 2$



$\lim_{x \rightarrow 1} f(x) = 2$

Since division by zero is not defined, $f(x) = \frac{x^2 - 1}{x - 1}$ is undefined when $x - 1 = 0$ or $x = 1$. Therefore there is a **discontinuity** in the graph when $x = 1$. Notice that $f(x) = \frac{x^2 - 1}{x - 1} = \frac{(x + 1)(x - 1)}{x - 1} = x + 1$, when $x \neq 1$

Even though $f(x) = \frac{x^2 - 1}{x - 1}$ is undefined when $x = 1$, the limit exists since as x becomes close to 1 from either side, $f(x)$ becomes close to 2.

x	0.8	0.9	0.99	0.999	1.001	1.01	1.1	1.2
$f(x)$	1.8	1.9	1.99	1.999	2.001	2.01	2.1	2.2

Note that $\lim_{x \rightarrow 1} \frac{x^2 - 1}{x - 1} = \lim_{x \rightarrow 1} \frac{(x + 1)(x - 1)}{x - 1} = \lim_{x \rightarrow 1} (x + 1) = 1 + 1 = 2$

Dec 21-10:59 AM

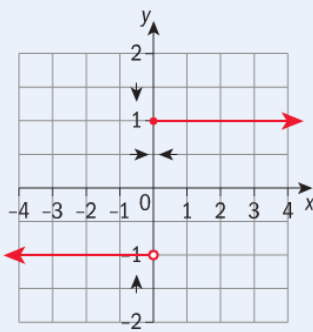
Use a GDC to examine each function graphically and numerically.

Find the limit or state that it does not exist.

- a $\lim_{x \rightarrow 2} x^2$ b $\lim_{x \rightarrow 1} \frac{x^2 - 1}{x - 1}$ c $\lim_{x \rightarrow 0} f(x)$; where $f(x) = \begin{cases} 1 & \text{for } x \geq 0 \\ -1 & \text{for } x < 0 \end{cases}$

C.)

$\lim_{x \rightarrow 0} f(x) = \text{DNE}$



$\lim_{x \rightarrow 0^+} f(x) = 1$

$\lim_{x \rightarrow 0^-} f(x) = -1$

$f(x)$ does not approach the same value as x approaches 0 from the left and right:

$\rightarrow 0 \leftarrow$

x	-0.2	-0.1	-0.01	-0.001	0.001	0.01	0.1	0.2
f(x)	-1	-1	-1	-1	1	1	1	1

Note that $f(0) = 1$, but $\lim_{x \rightarrow 0} f(x)$ does not exist.

This is because $f(x)$ is close to 1 for values of x to the right of $x = 0$ and $f(x)$ is close to -1 for values of x to the left of $x = 0$.

Dec 21-10:59 AM



Exercise 7B

Use a GDC to examine each function graphically and numerically. Find the limit or state that it does not exist.

1 $\lim_{x \rightarrow 3} (x^2 + 1)$

2 $\lim_{x \rightarrow 0} \frac{x^3 - 4x^2 + x}{x}$

3 $\lim_{x \rightarrow 2} \frac{x^2 - 3x + 2}{x - 2}$

4 $\lim_{x \rightarrow 4} \frac{1}{x - 4}$

5 $\lim_{x \rightarrow 1} f(x)$; where $f(x) = \begin{cases} x + 3 & \text{for } x \geq 1 \\ -x + 5 & \text{for } x < 1 \end{cases}$

6 $\lim_{x \rightarrow 2} f(x)$; where $f(x) = \begin{cases} x^2 + 3 & \text{for } x \geq 2 \\ x & \text{for } x < 2 \end{cases}$

Feb 24-10:13 AM